

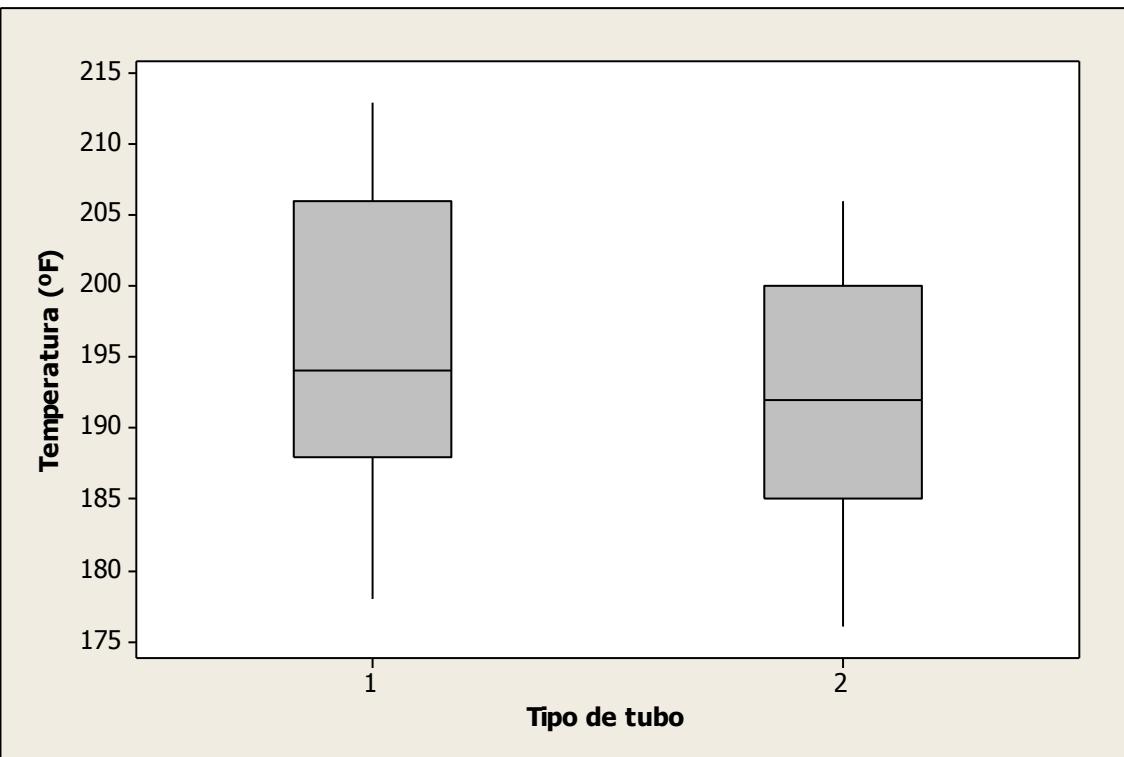
Lista nº 3 – Inferência Estatística para 2 Amostras
Algumas Soluções Computacionais

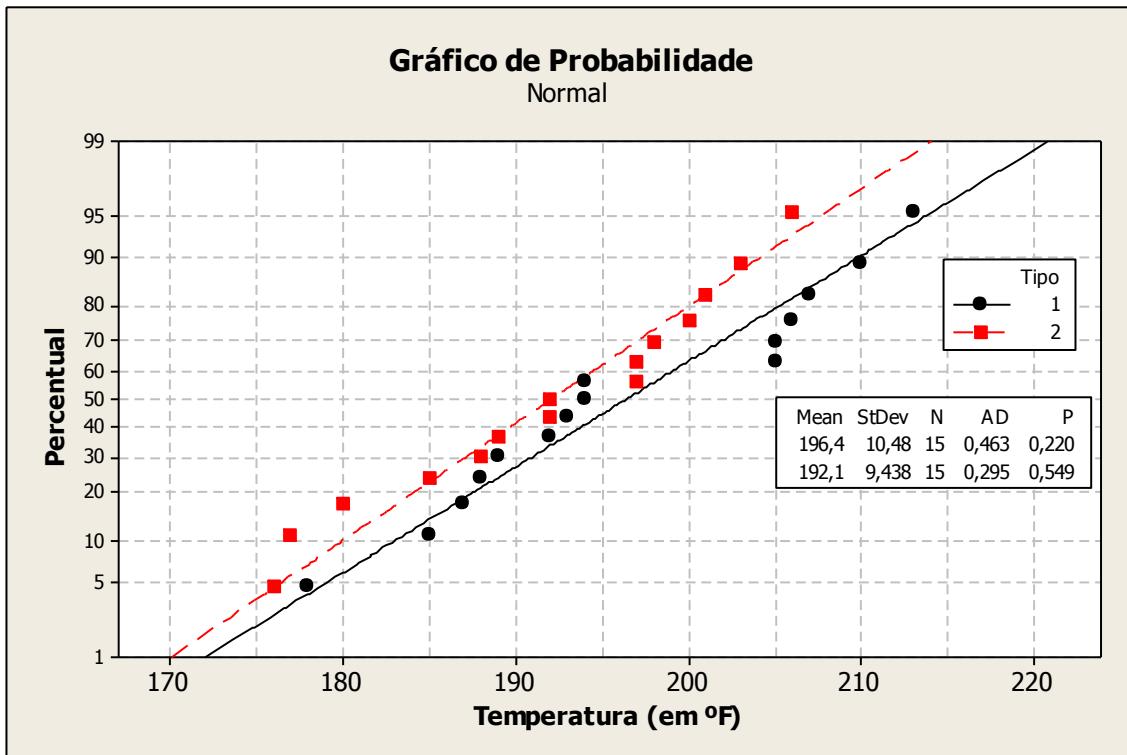
Exercício 5-1:

Descriptive Statistics: Volume

Variable	Máquina	N	N*	Mean	SE Mean	StDev	Minimum	Q1	Median
Volume	1	10	0	16,015	0,00957	0,0303	15,960	15,988	16,020
	2	10	0	16,005	0,00806	0,0255	15,960	15,985	16,010
Variable	Máquina			Q3	Maximum				
Volume	1			16,043	16,050				

Exercício 5-16.





Two-Sample T-Test and CI: Temperatura; Tipo

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Two-sample T for Temperatura
  
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Tipo	N	Mean	StDev	SE Mean
1	15	196,4	10,5	2,7
2	15	192,07	9,44	2,4

```
Difference = mu (1) - mu (2)
Estimate for difference: 4,33
95% upper bound for difference: 10,53
T-Test of difference = 0 (vs <): T-Value = 1,19  P-Value = 0,878  DF = 28
Both use Pooled StDev = 9,9723
```

Power and Sample Size

2-Sample t Test

```
Testing mean 1 = mean 2 (versus <)
Calculating power for mean 1 = mean 2 + difference
Alpha = 0,05  Assumed standard deviation = 9,9723
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Difference	Sample Size	Power
-5	15	0,380196

The sample size is for each group.

Power and Sample Size

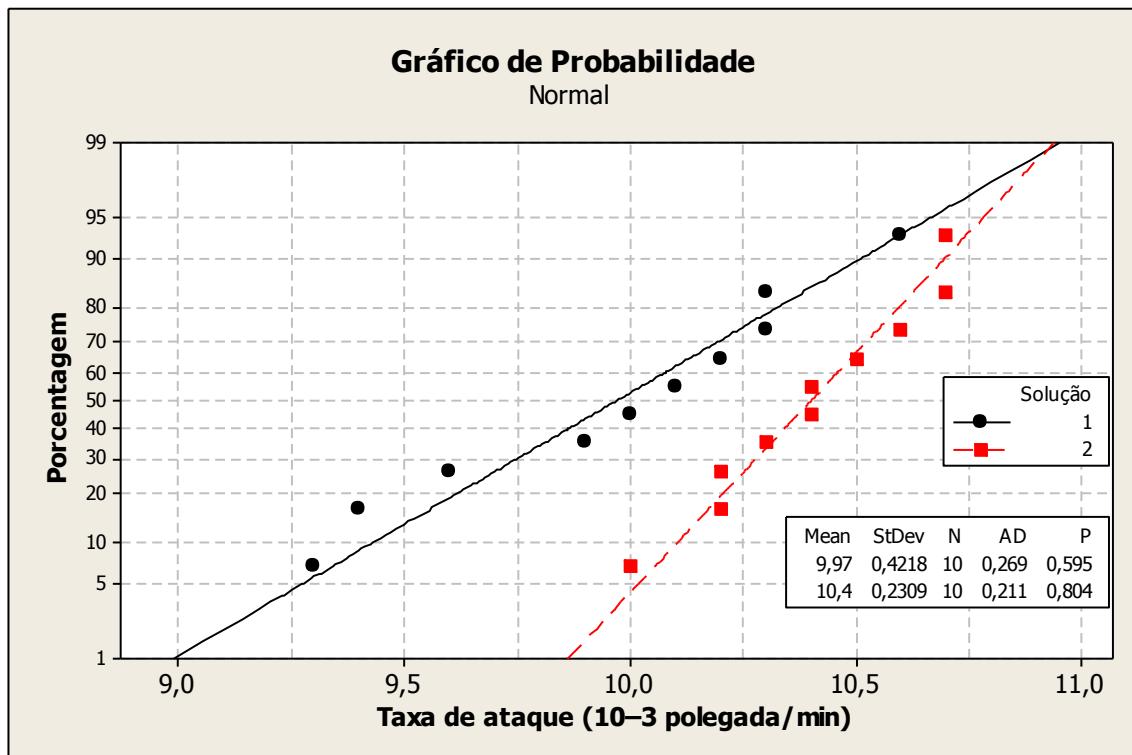
2-Sample t Test

Testing mean 1 = mean 2 (versus <)
 Calculating power for mean 1 = mean 2 + difference
 Alpha = 0,05 Assumed standard deviation = 9,9723

	Sample	Target	
Difference	Size	Power	Actual Power
-5	69	0,9	0,900681

The sample size is for each group.

Exercício 5-17



Test and CI for Two Variances: Taxa de ataque vs Solução

Method

Null hypothesis Variance(1) / Variance(2) = 1
 Alternative hypothesis Variance(1) / Variance(2) not = 1
 Significance level Alpha = 0,05

Statistics

Solução	N	StDev	Variance
1	10	0,422	0,178
2	10	0,231	0,053

Ratio of standard deviations = 1,826
 Ratio of variances = 3,335

95% Confidence Intervals

Distribution	CI for StDev	CI for Variance
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of Data	Ratio	Ratio
Normal	(0,910; 3,664)	(0,828; 13,428)
Continuous	(0,818; 3,982)	(0,670; 15,854)

Tests

Method	Test
F Test (normal)	DF1 DF2 Statistic P-Value
Levene's Test (any continuous)	9 9 3,34 0,087
	1 18 2,77 0,114

Two-Sample T-Test and CI: Taxa de ataque; Solução

Two-sample T for Taxa de ataque

Solução	N	Mean	StDev	SE Mean
1	10	9,970	0,422	0,13
2	10	10,400	0,231	0,073

```
Difference = mu (1) - mu (2)
Estimate for difference: -0,430
95% CI for difference: (-0,749; -0,111)
T-Test of difference = 0 (vs not =): T-Value = -2,83 P-Value = 0,011 DF = 18
Both use Pooled StDev = 0,3400
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Exercício 5-22

Two-Sample T-Test and CI

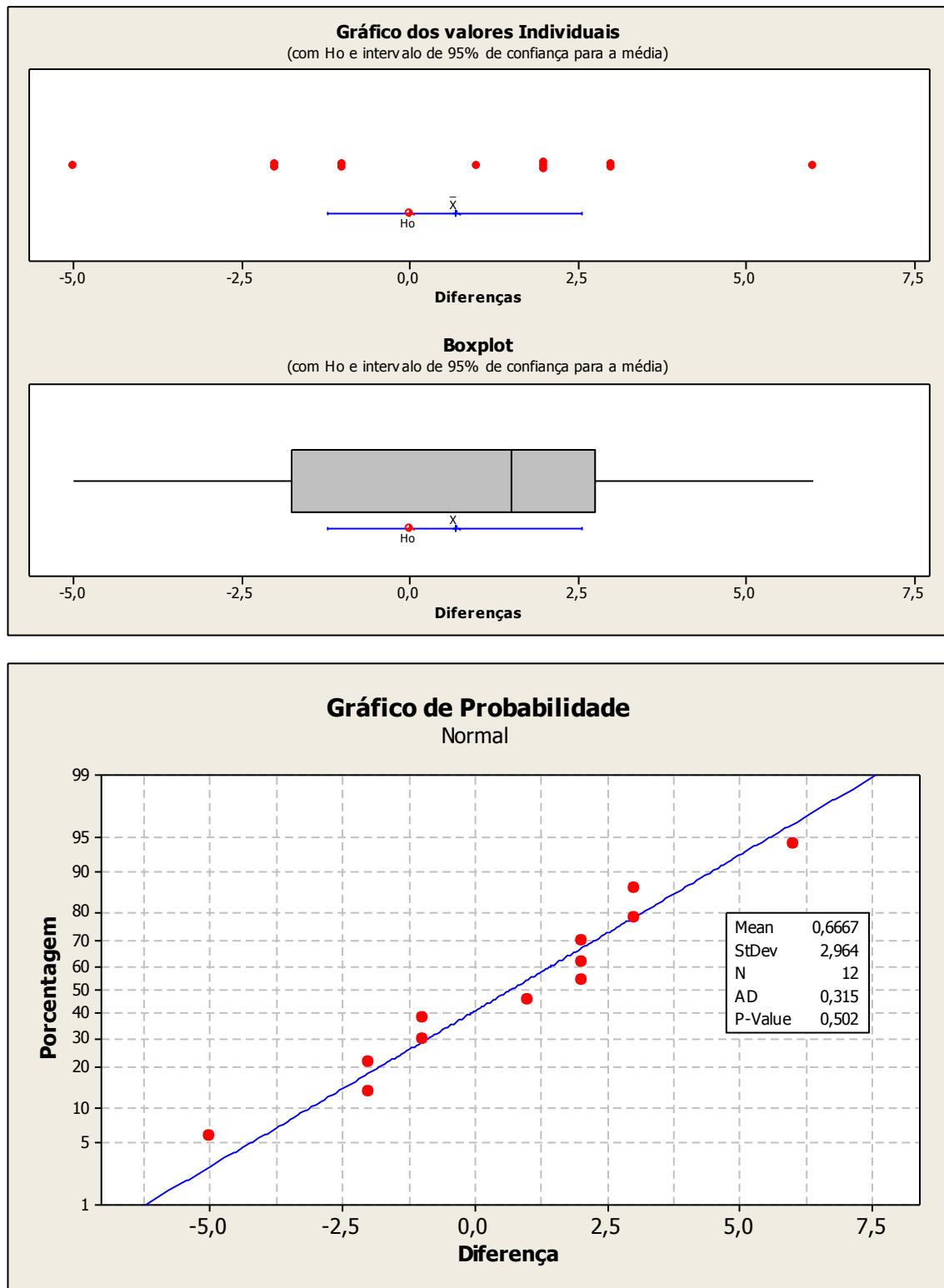
Sample	N	Mean	StDev	SE Mean
1	25	20,12	1,90	0,38
2	25	11,64	7,90	1,6

```
Difference = mu (1) - mu (2)
Estimate for difference: 8,48
95% CI for difference: (5,14; 11,82)
T-Test of difference = 0 (vs not =): T-Value = 5,22 P-Value = 0,000 DF = 26
```

Two-Sample T-Test and CI

Sample	N	Mean	StDev	SE Mean
1	25	20,12	1,90	0,38
2	25	11,64	7,90	1,6

```
Difference = mu (1) - mu (2)
Estimate for difference: 8,48
95% lower bound for difference: 5,71
```

Exercício 5-31

Paired T-Test and CI: Linguagem 1; Linguagem 2

Paired T for Linguagem 1 - Linguagem 2

	N	Mean	StDev	SE Mean
Linguagem 1	12	17,92	3,63	1,05

Linguagem	2	12	17,25	4,59	1,33
Difference		12	0,667	2,964	0,856

95% CI for mean difference: (-1,217; 2,550)
T-Test of mean difference = 0 (vs not = 0): T-Value = 0,78 P-Value = 0,452

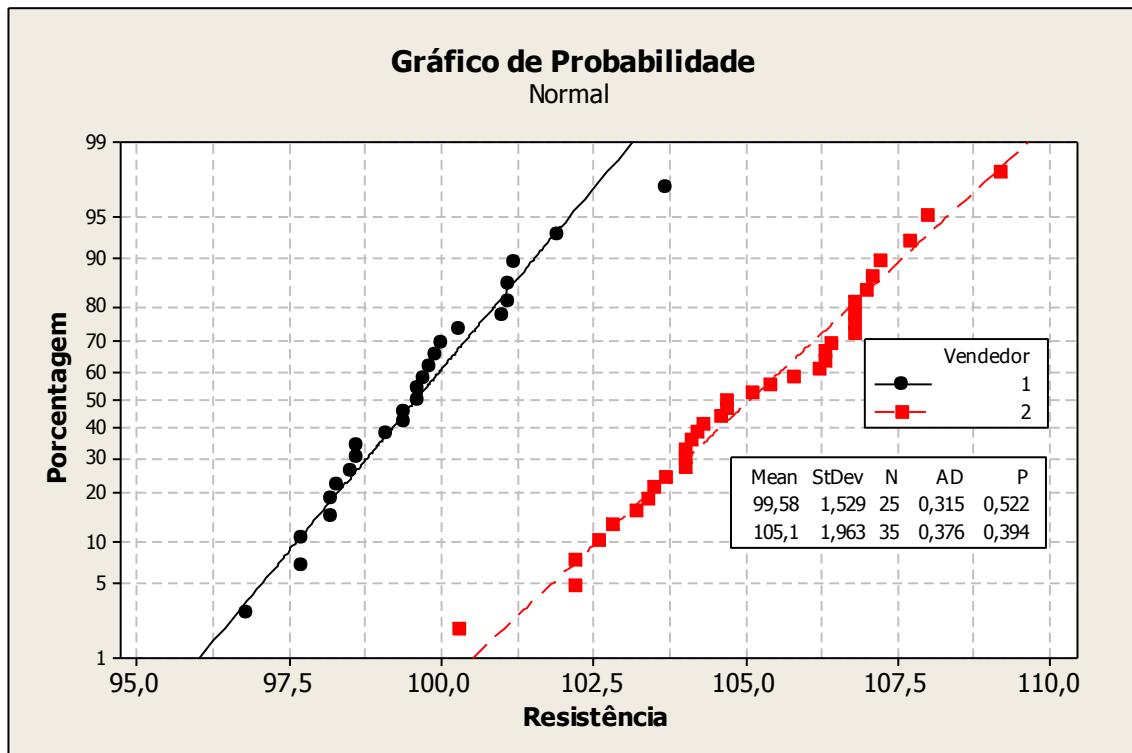
Exercício 5-32

Paired T-Test and CI: Antes; Depois

Paired T for Antes - Depois

	N	Mean	StDev	SE Mean
Antes	15	261,80	24,96	6,45
Depois	15	234,93	10,48	2,71
Difference	15	26,87	19,04	4,92

95% CI for mean difference: (16,32; 37,41)
T-Test of mean difference = 0 (vs not = 0): T-Value = 5,47 P-Value = 0,000

Exercício 5-67:

Test and CI for Two Variances: Resistência vs Vendedor

Method

Null hypothesis $\text{Variance}(1) / \text{Variance}(2) = 1$
 Alternative hypothesis $\text{Variance}(1) / \text{Variance}(2) \neq 1$
 Significance level Alpha = 0,05

Statistics

Vendedor	N	StDev	Variance
1	25	1,529	2,338
2	35	1,963	3,852

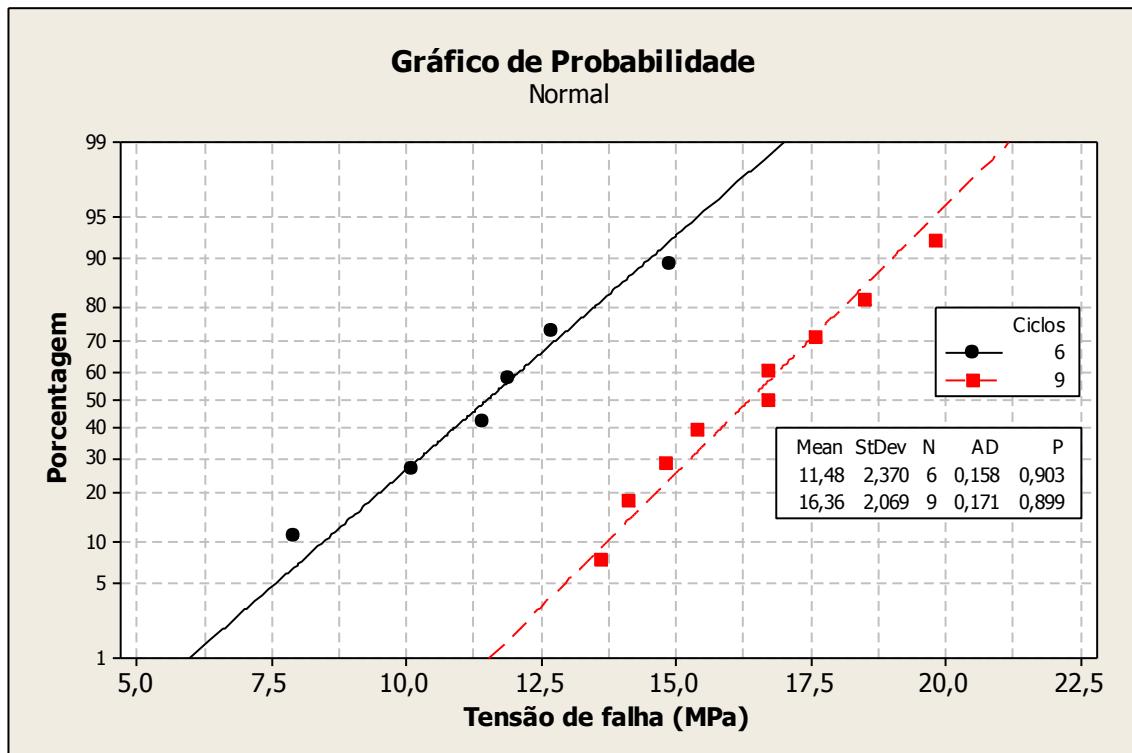
Ratio of standard deviations = 0,779
 Ratio of variances = 0,607

95% Confidence Intervals

Distribution of Data	CI for StDev		CI for Variance	
	Normal	Continuous	Ratio	Ratio
Normal	(0,541; 1,150)		(0,293; 1,323)	
Continuous		(0,467; 1,061)		(0,218; 1,126)

Tests

Method	Test			
	DF1	DF2	Statistic	P-Value
F Test (normal)	24	34	0,61	0,205
Levene's Test (any continuous)	1	58	2,97	0,090

Exercícios 5-68 e 5-69:

Test and CI for Two Variances: Tensão de falha vs Ciclos

Method

Null hypothesis $\text{Variance}(6) / \text{Variance}(9) = 1$
 Alternative hypothesis $\text{Variance}(6) / \text{Variance}(9) \neq 1$
 Significance level Alpha = 0,05

Statistics

Ciclos	N	StDev	Variance
6	6	2,370	5,618
9	9	2,069	4,283

Ratio of standard deviations = 1,145
 Ratio of variances = 1,312

95% Confidence Intervals

Distribution of Data	CI for StDev		CI for Variance	
	Ratio	Ratio	Ratio	Ratio
Normal	(0,522; 2,977)		(0,272; 8,863)	
Continuous	(0,344; 3,229)		(0,119; 10,426)	

Tests

Method	Test			
	DF1	DF2	Statistic	P-Value
F Test (normal)	5	8	1,31	0,697
Levene's Test (any continuous)	1	13	0,01	0,944

Two-Sample T-Test and CI: Tensão de falha; Ciclos

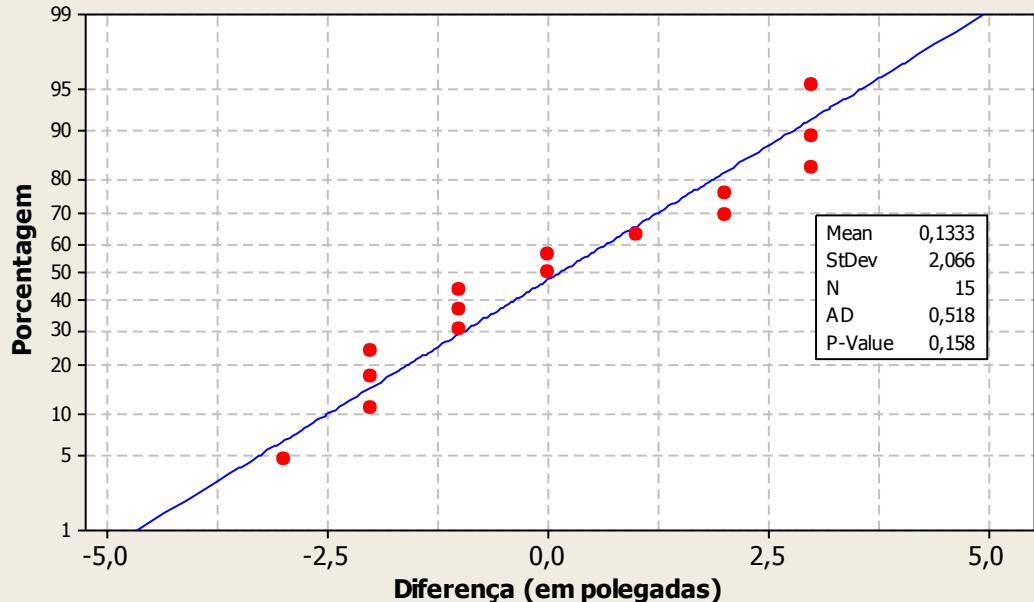
Two-sample T for Tensão de falha

Ciclos	N	Mean	StDev	SE Mean
6	6	11,48	2,37	0,97
9	9	16,36	2,07	0,69

Difference = mu (6) - mu (9)
 Estimate for difference: -4,87
 99% CI for difference: (-8,35; -1,40)
 T-Test of difference = 0 (vs not =): T-Value = -4,22 P-Value = 0,001 DF = 13
 Both use Pooled StDev = 2,1900

Exercício 5-85

Gráfico de Probabilidade
Normal



Paired T-Test and CI: Medidor 1; Medidor 2

Paired T for Medidor 1 - Medidor 2

	N	Mean	StDev	SE Mean
Medidor 1	15	49,200	3,144	0,812
Medidor 2	15	49,067	3,411	0,881
Difference	15	0,133	2,066	0,533

95% CI for mean difference: (-1,011; 1,277)
 T-Test of mean difference = 0 (vs not = 0): T-Value = 0,25 P-Value = 0,806

Power and Sample Size

Paired t Test

Testing mean paired difference = 0 (versus not = 0)

Calculating power for mean paired difference = difference

Alpha = 0,01 Assumed standard deviation of paired differences = 2,066

Difference	Sample Size	Target Power	Actual Power
1,65	22	0,8	0,807867